

In-Depth DCT Coefficient Distribution Analysis for First Quantization Estimation


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FQE: First Quantization Estimation


RAW IMAGE



Q1

12	8	8	12	17	21	24	17
8	9	9	11	15	19	12	12
8	9	10	12	19	12	12	12
12	11	12	21	12	12	12	12
17	15	19	12	12	12	12	12
21	19	12	12	12	12	12	12
24	12	12	12	12	12	12	12
17	12	12	12	12	12	12	12

JPEG COMPRESSED



Q2

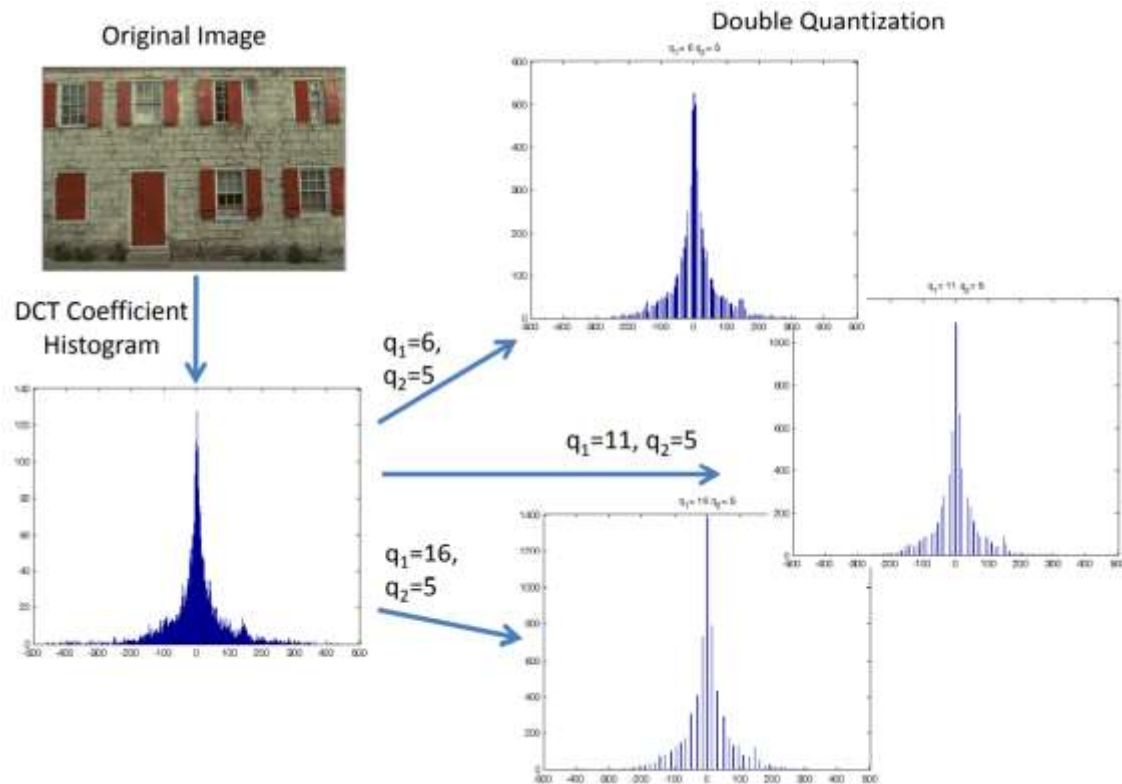
12	8	8	12	17	21	24	17
8	9	9	11	15	19	12	12
8	9	10	12	19	12	12	12
12	11	12	21	12	12	12	12
17	15	19	12	12	12	12	12
21	19	12	12	12	12	12	12
24	12	12	12	12	12	12	12
17	12	12	12	12	12	12	12

JPEG COMPRESSED



FQE

State-of-the-art



Consecutive quantizations introduced periodic artifacts into the histogram of DCT coefficients.

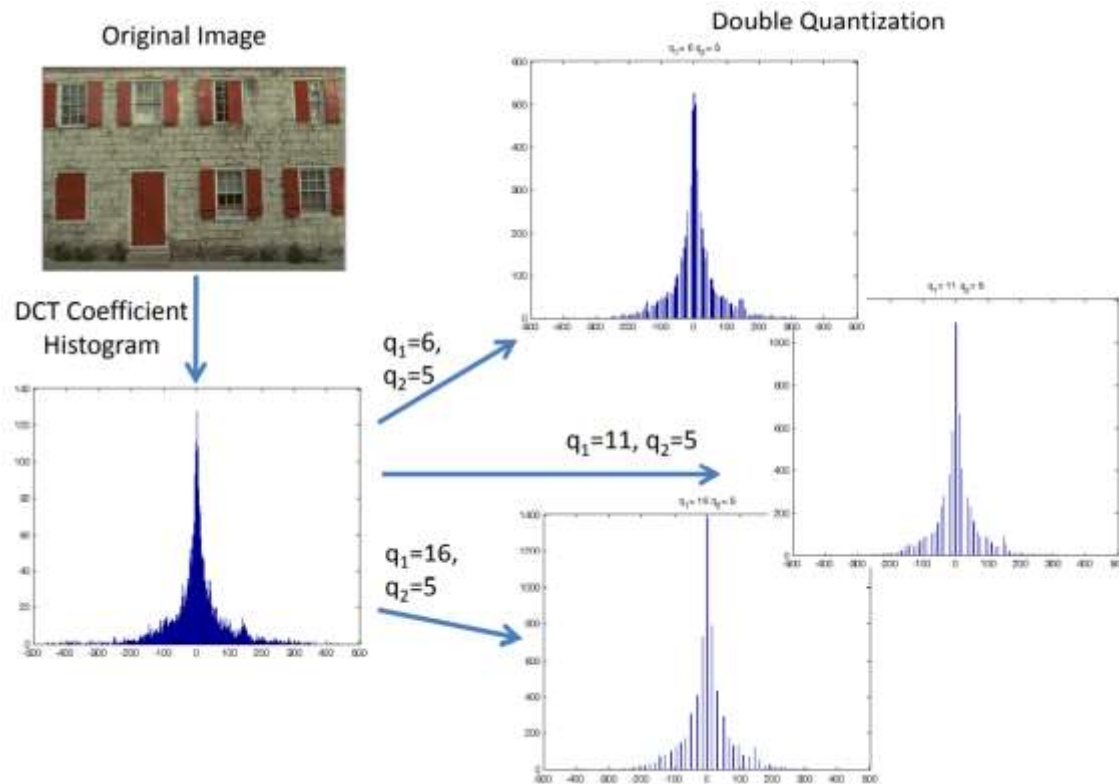
T. Bianchi and A. Piva, "Image forgery localization via block-grained analysis of JPEG artifacts," *Proc. of IEEE Trans. on Information Forensics and Security*, vol. 7, no. 3, p. 1003, 2012.

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Y. Niu, B. Tondi, Y. Zhao, and M. Barni, "Primary quantization matrix estimation of double compressed JPEG images via CNN," *IEEE Signal Processing Letters*, vol. 27, pp. 191–195, 2020.

State-of-the-art



Statistical approaches

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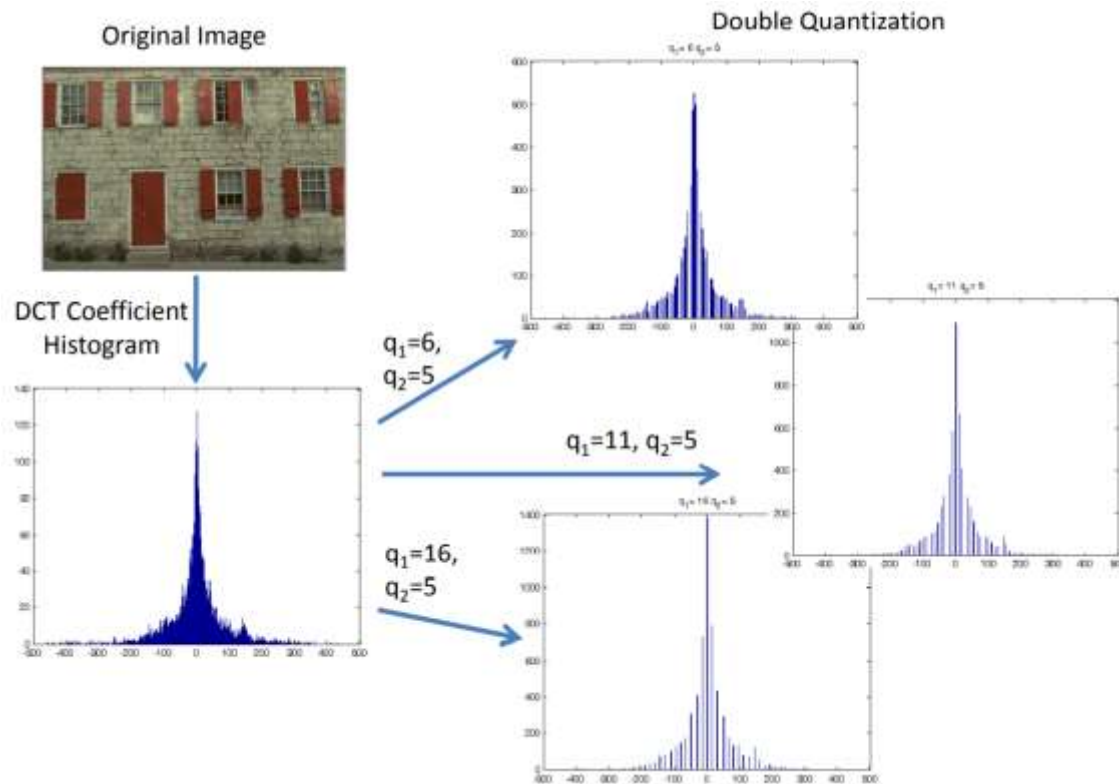
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State-of-the-art



Statistical approaches

They usually provide satisfactory results only at specific combinations between first and second compression factors.

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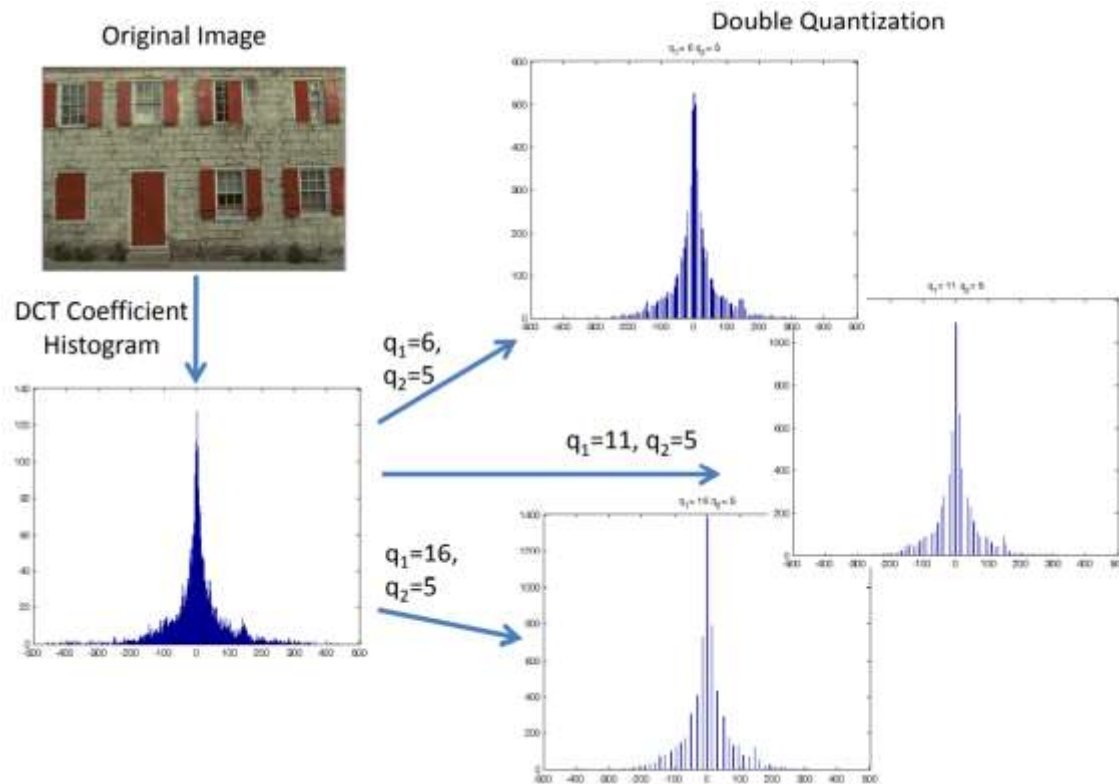
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Machine learning approaches

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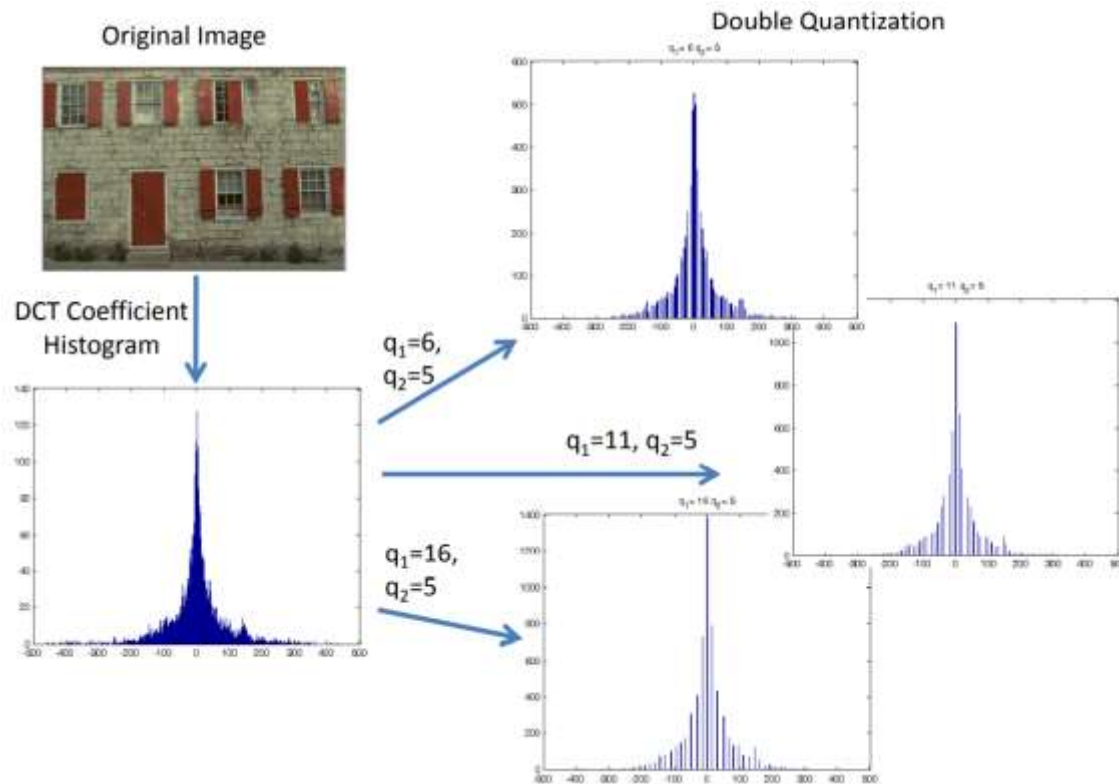
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State-of-the-art



Statistical approaches

They usually provide satisfactory results only at specific combinations between first and second compression factors.

Machine learning approaches

They could suffer from overfitting.

Consecutive quantizations introduced periodic artifacts into the histogram of DCT coefficients.

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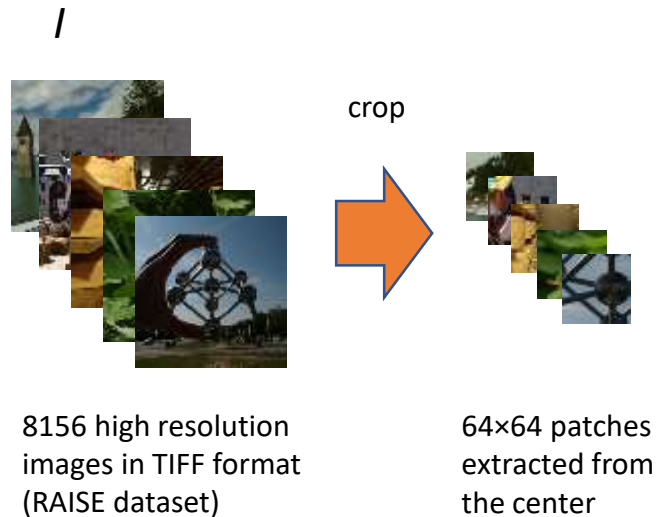
Training Dataset Generation

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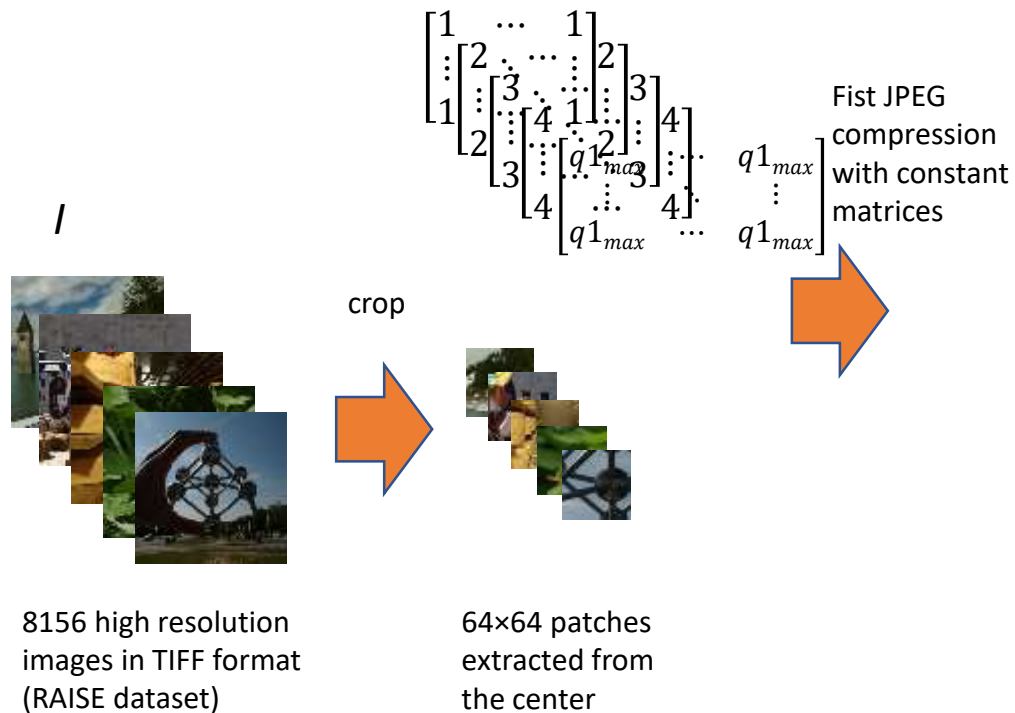


8156 high resolution
images in TIFF format
(RAISE dataset)

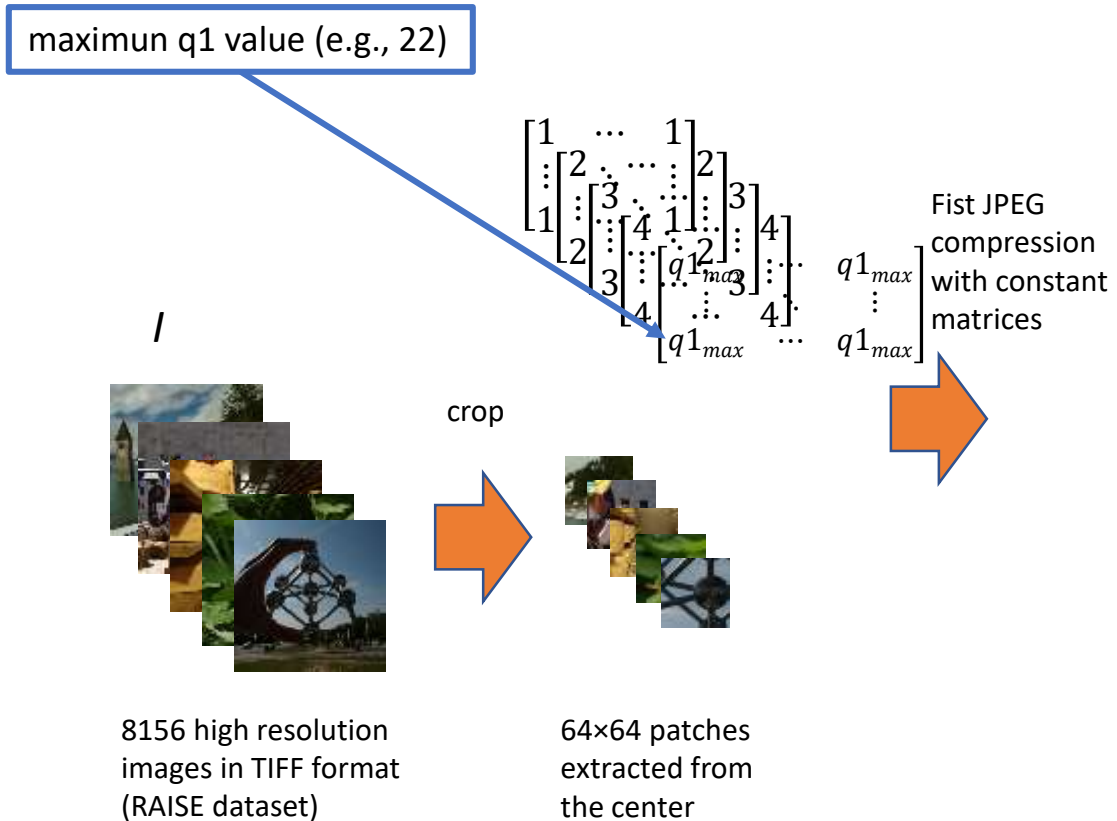
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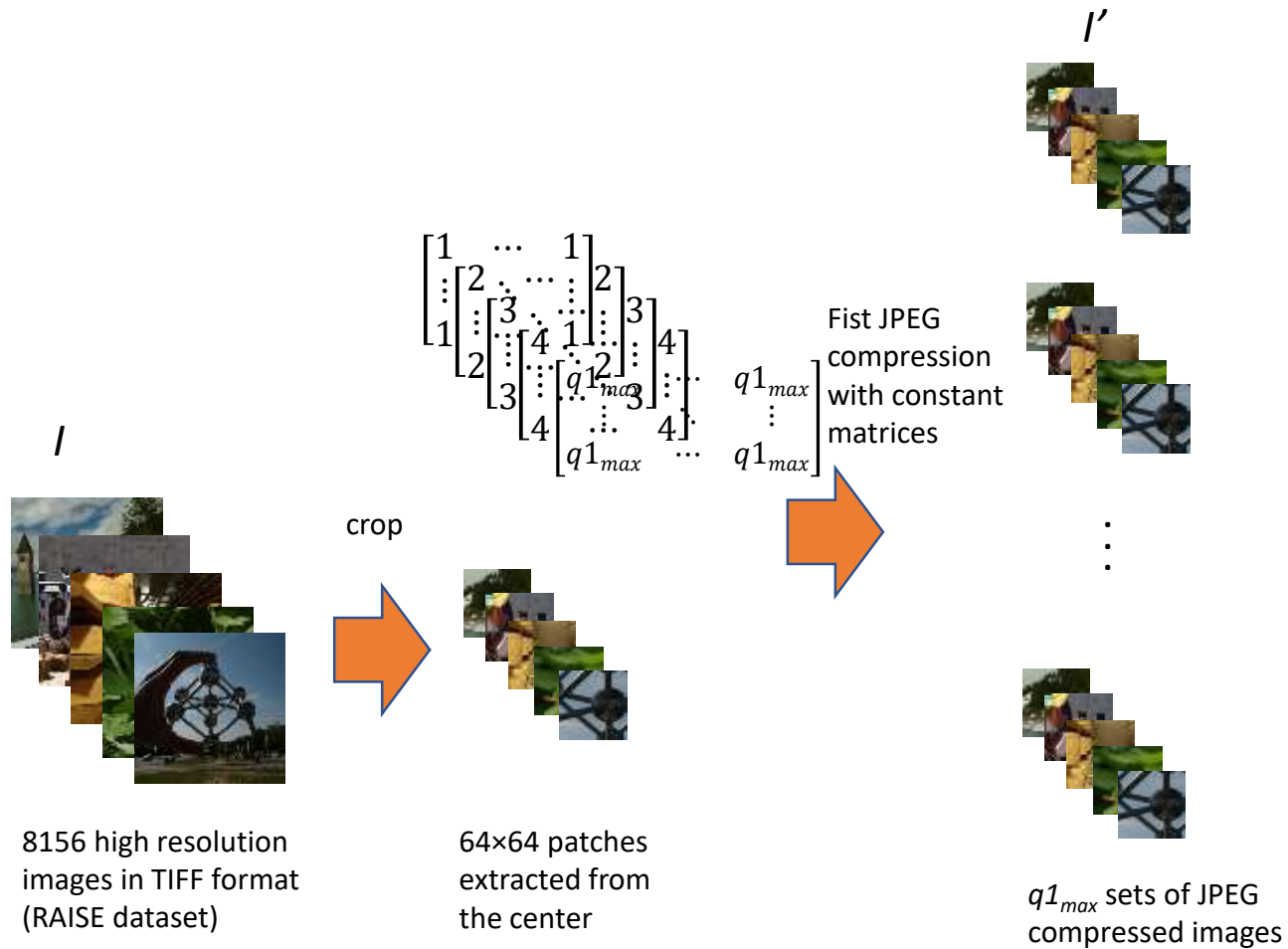
Training Dataset Generation



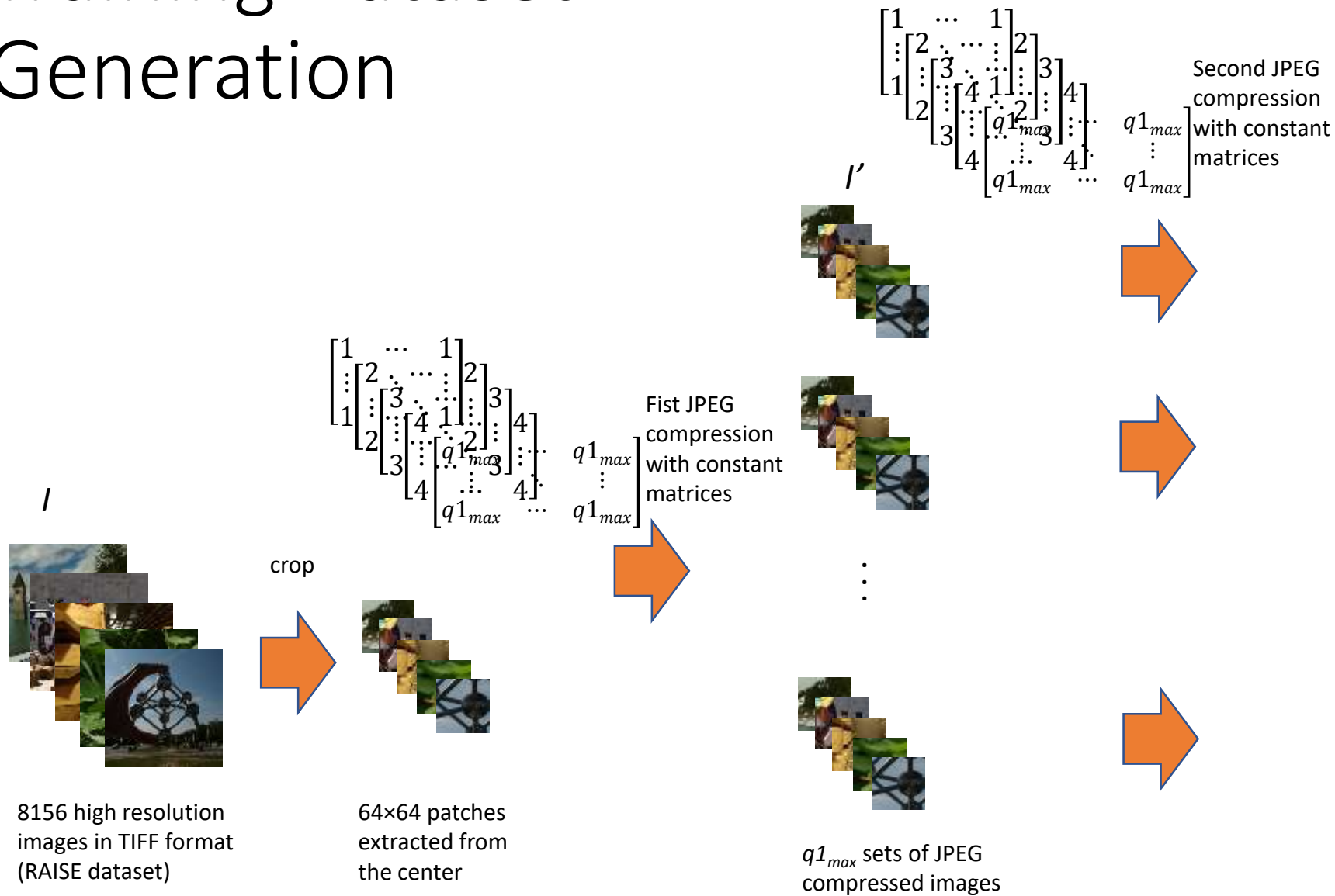
Training Dataset Generation



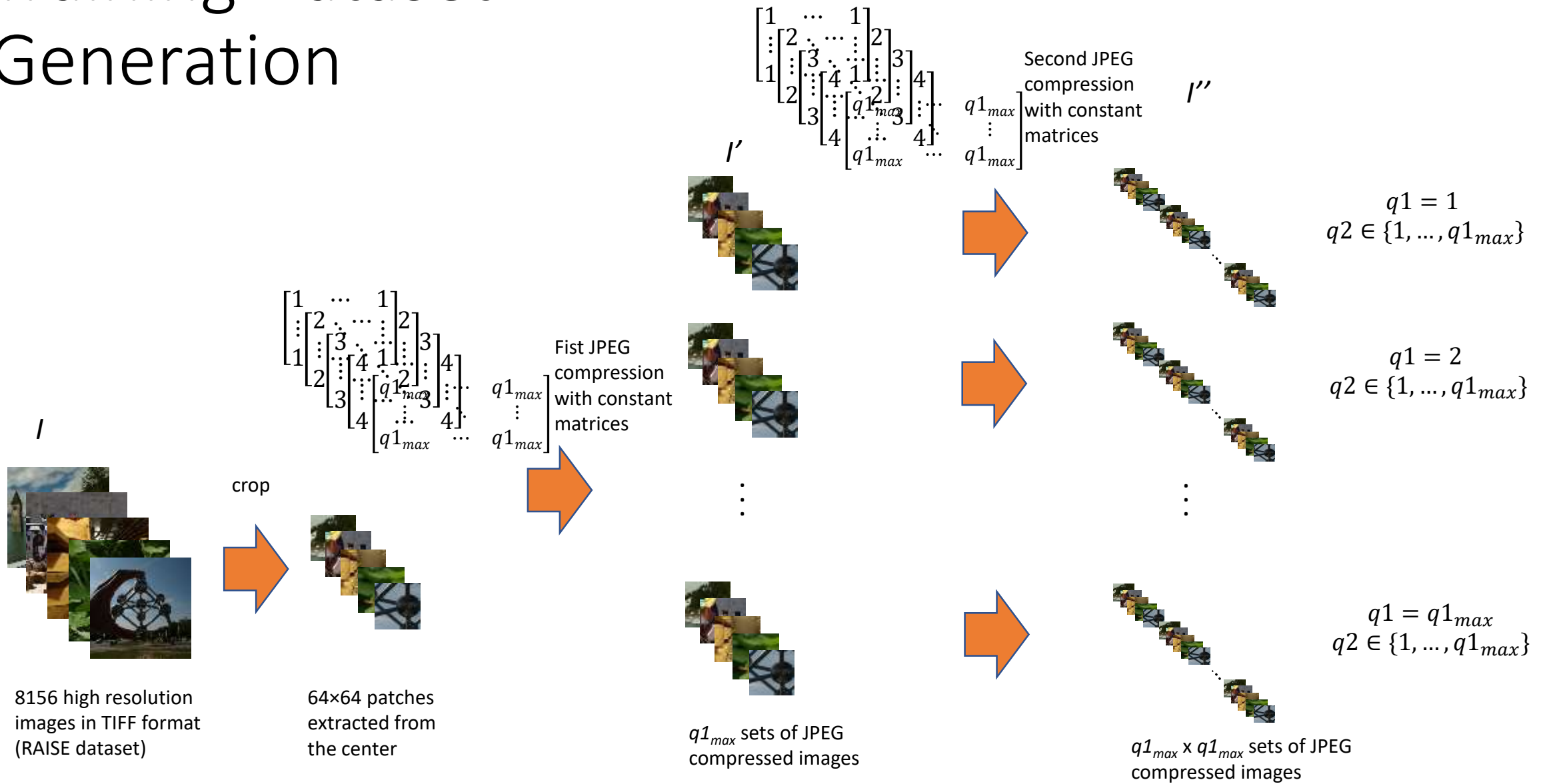
Training Dataset Generation



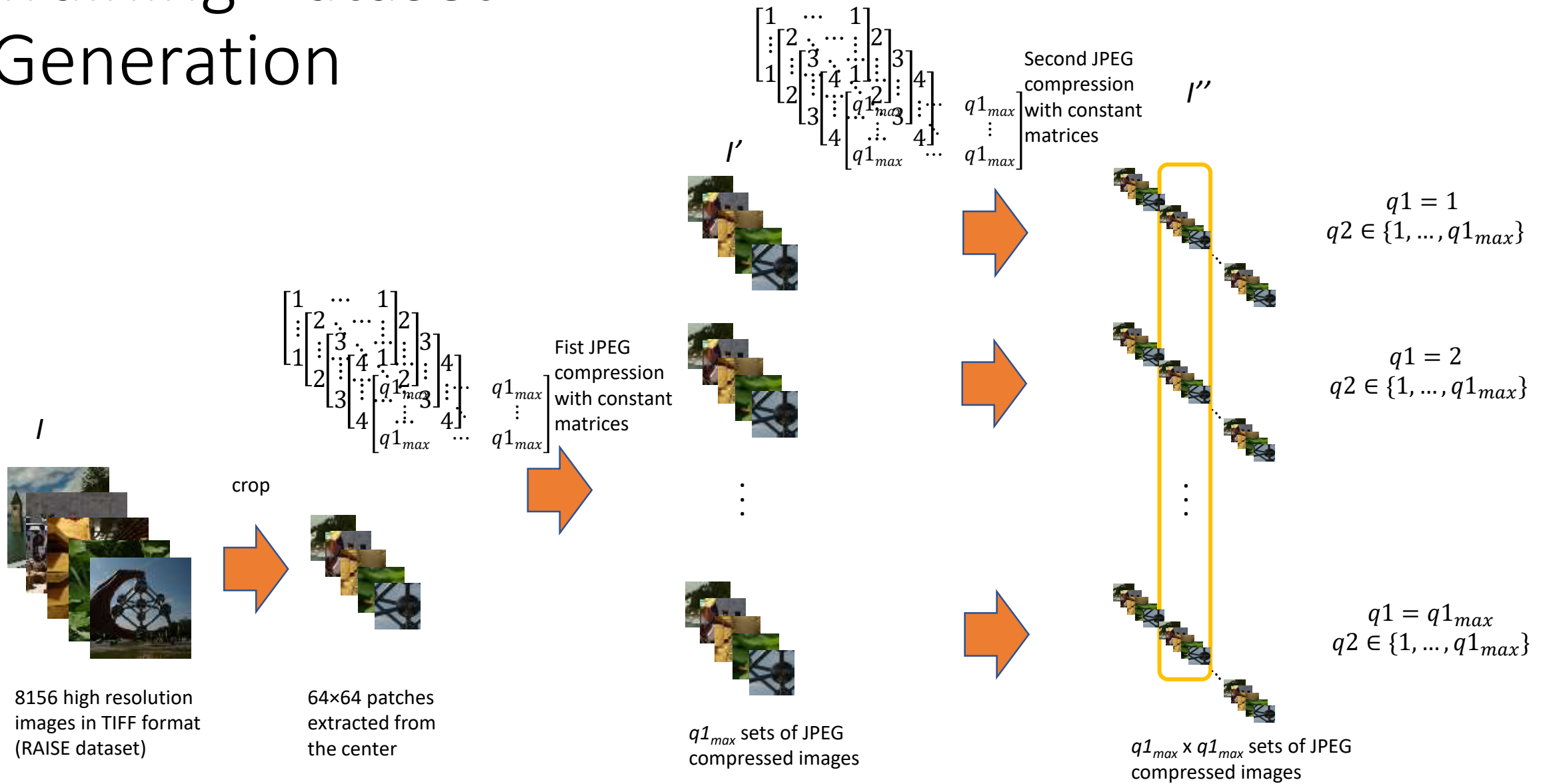
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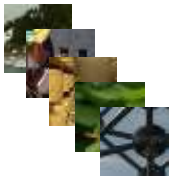
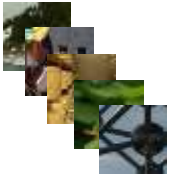


Training Dataset Generation

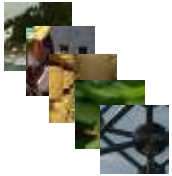


Training Dataset Generation

I''



\vdots

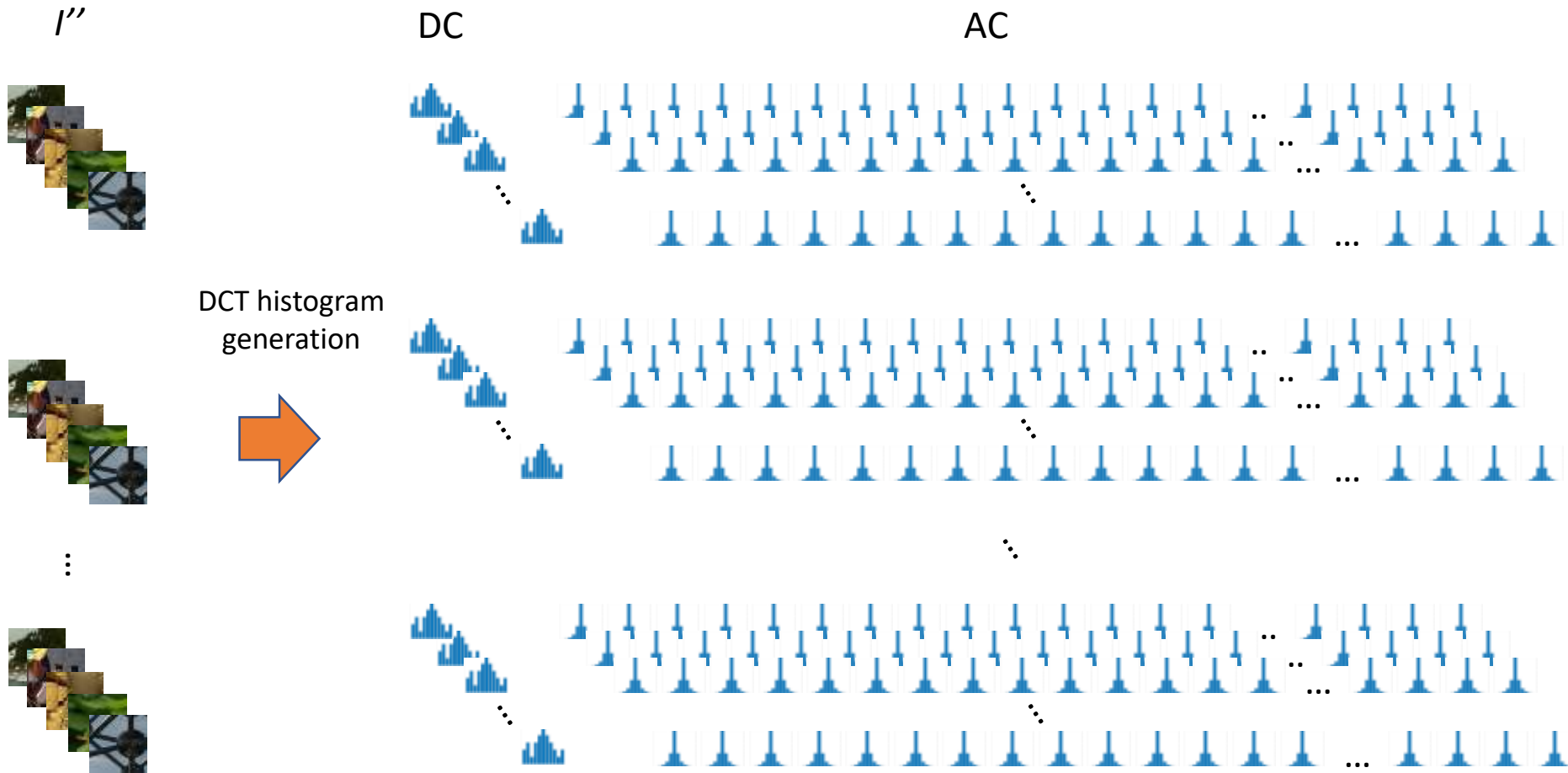


Double compressed images with

$q1 \in \{1, \dots, q1_{max}\}$

$q2 = q2_i$

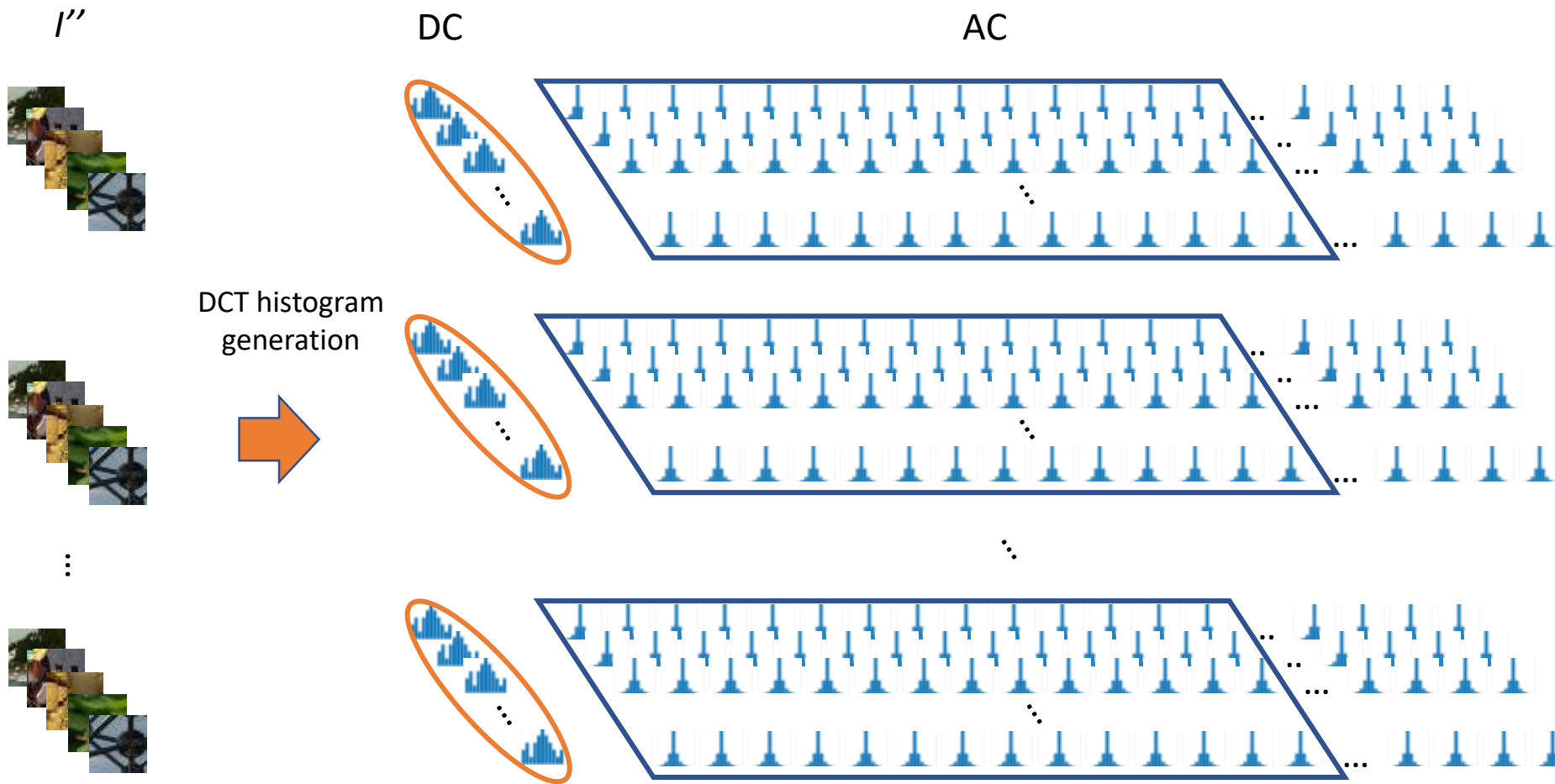
Training Dataset Generation



Double compressed images with
 $q1 \in \{1, \dots, q1_{max}\}$
 $q2 = q2_i$

DCT histograms

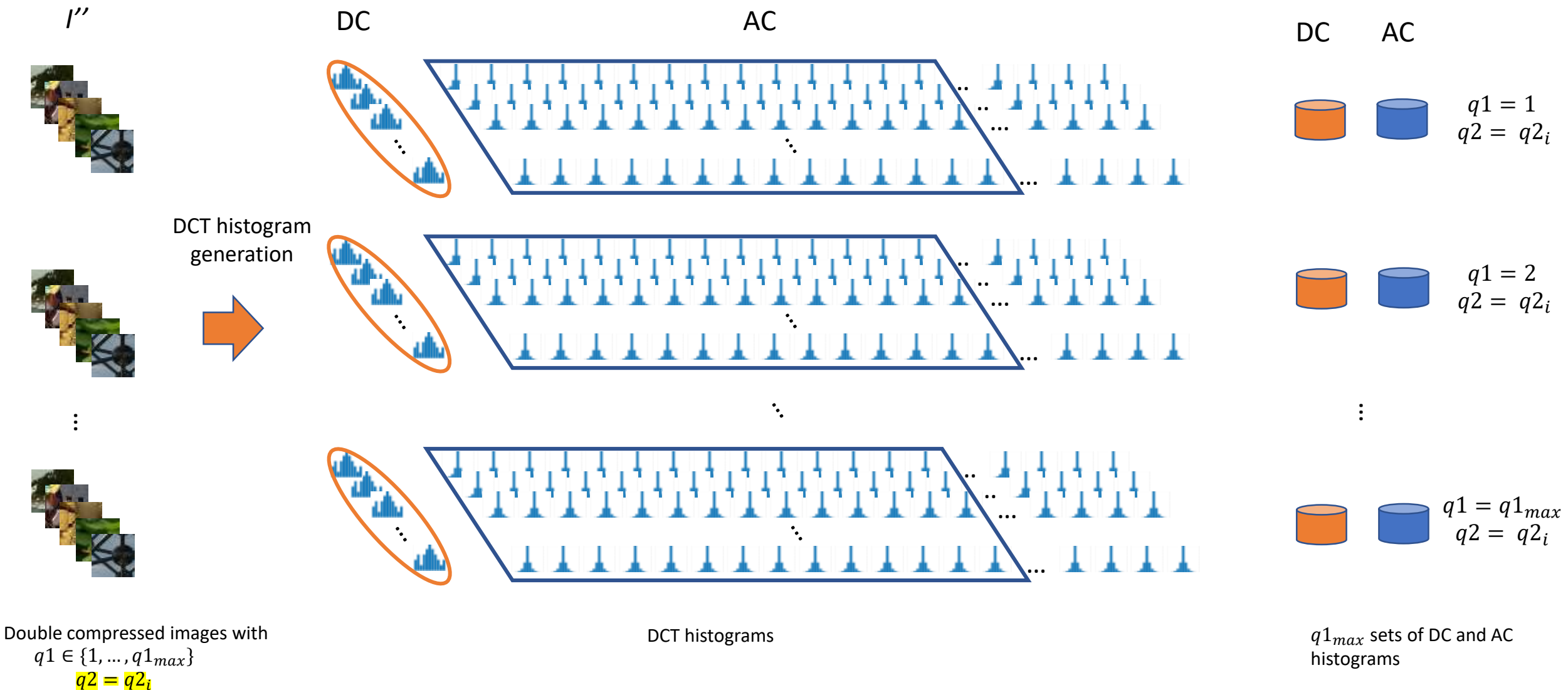
Training Dataset Generation



Double compressed images with
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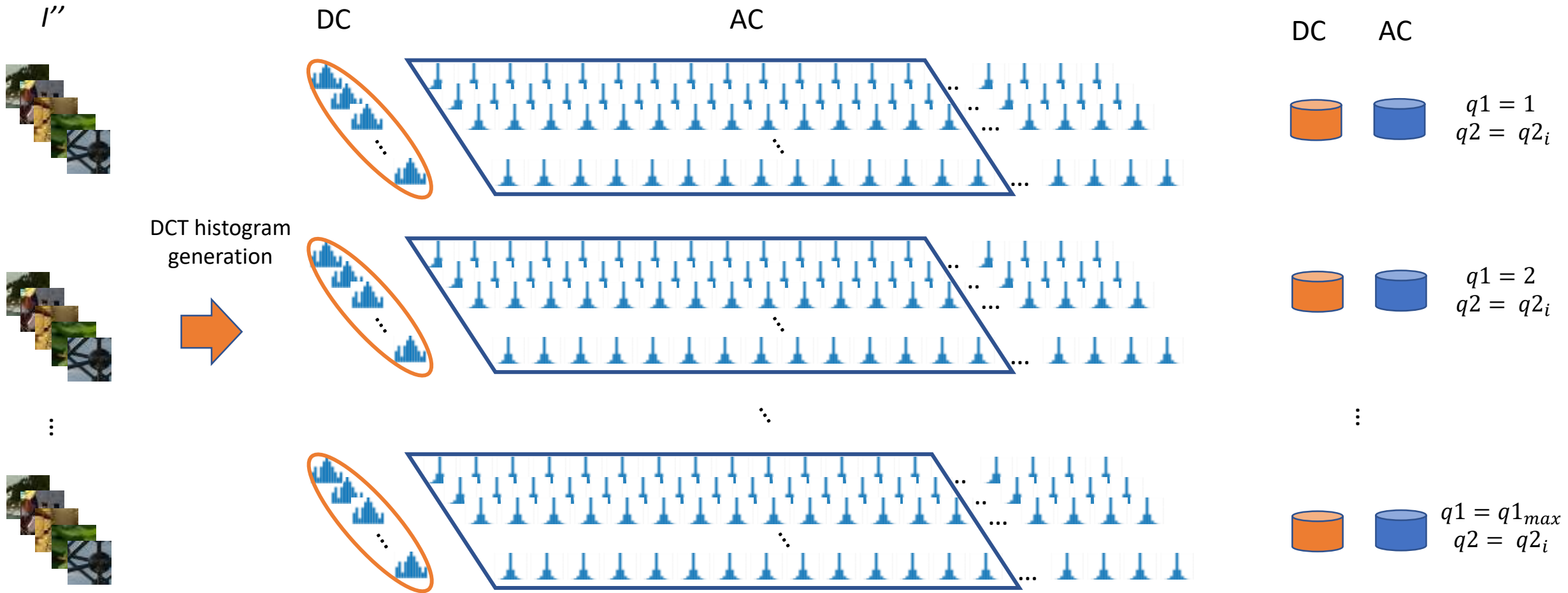
DCT histograms

Training Dataset Generation



Training Dataset Generation

Considering all the q_2 in the range $\{1, \dots, q_{1_{max}}\}$, $q_{1_{max}} \times q_{1_{max}}$ sets of DC and AC histograms are generated.



Double compressed images with $q_1 \in \{1, \dots, q_{1_{max}}\}$
 $q_2 = q_{2_i}$

DCT histograms

$q_{1_{max}}$ sets of DC and AC histograms

Algorithm 1 The Proposed FQE Technique

Input: double compressed image I''

Output: $\{q1_1, q1_2, \dots, q1_k\}$

Initialization : $k, q1_{max}$

1: **for** $i = 1$ to k **do**

2: h_i : distribution of i -th DCT coefficient

3: **if** ($i = 1$) **then**

4: D : DC_{dset}

5: m : median value of h_i

6: **else**

7: D : AC_{dset}

8: β : β fitted on Laplacian h_i

9: **end if**

10: $q2_i$: quantization factor of Q_2 for i -th DCT

11: **for** $j = 1$ to $q1_{max}$ **do**

12: $D_{j,q2_i}$: sub-dataset ($q1, q2$) with $q1 = j, q2 = q2_i$

13: $D_{j,q2_i}(m, \beta)$: sub-range with most similar m, β

14: $d_{i,j}$: lower χ^2 distance between h_i and $D_{j,q2_i}$

15: **end for**

16: $q1_i$: $\arg \min_{\{d_{i,j}\}}, j \in \{1, 2, \dots, q1_{max}\}$

17: **end for**

18: regularize($\{q1_1, q1_2, \dots, q1_k\}$)

19: **return** $\{q1_1, q1_2, \dots, q1_k\}$

Algorithm 1 The Proposed FQE Technique

Input: double compressed image I'' **Output:** $\{q1_1, q1_2, \dots, q1_k\}$ *Initialization* : $k, q1_{max}$ 1: **for** $i = 1$ to k **do**2: h_i : distribution of i -th DCT coefficient3: **if** ($i = 1$) **then**4: D : DC_{dset} 5: m : median value of h_i 6: **else**7: D : AC_{dset} 8: β : β fitted on Laplacian h_i 9: **end if**10: $q2_i$: quantization factor of Q_2 for i -th DCT11: **for** $j = 1$ to $q1_{max}$ **do**12: $D_{j,q2_i}$: sub-dataset ($q1, q2$) with $q1 = j, q2 = q2_i$ 13: $D_{j,q2_i}(m, \beta)$: sub-range with most similar m, β 14: $d_{i,j}$: lower χ^2 distance between h_i and $D_{j,q2_i}$ 15: **end for**16: $q1_i$: $\arg \min_{\{d_{i,j}\}, j \in \{1, 2, \dots, q1_{max}\}}$ 17: **end for**18: regularize($\{q1_1, q1_2, \dots, q1_k\}$)19: **return** $\{q1_1, q1_2, \dots, q1_k\}$



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$$\begin{bmatrix} \dots \\ \vdots \\ \dots \end{bmatrix}$$
First quantization matrix Q_1

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number of quantization factors
to be estimated (e.g., 15)

maximun q1 value (e.g., 22)



```
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2:    $h_i$  : distribution of  $i$ -th DCT coefficient
3:   if ( $i = 1$ ) then
4:      $D$  :  $DC_{dset}$ 
5:      $m$  : median value of  $h_i$ 
6:   else
7:      $D$  :  $AC_{dset}$ 
8:      $\beta$  :  $\beta$  fitted on Laplacian  $h_i$ 
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18: regularize( $\{q1_1, q1_2, \dots, q1_k\}$ )
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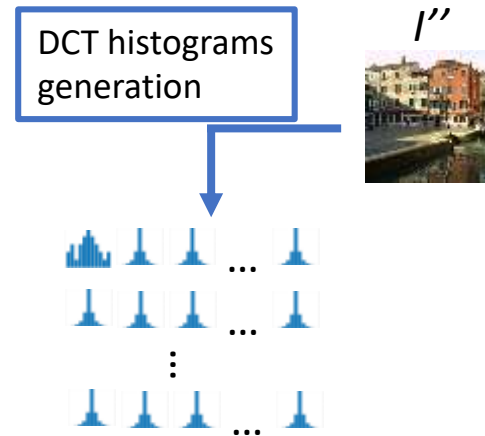
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First quantization matrix Q_1

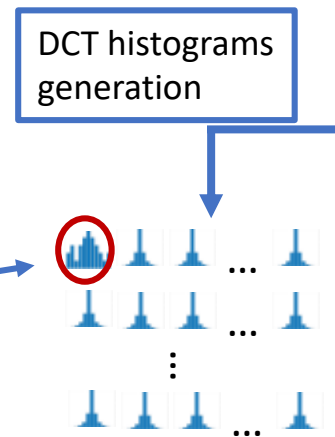
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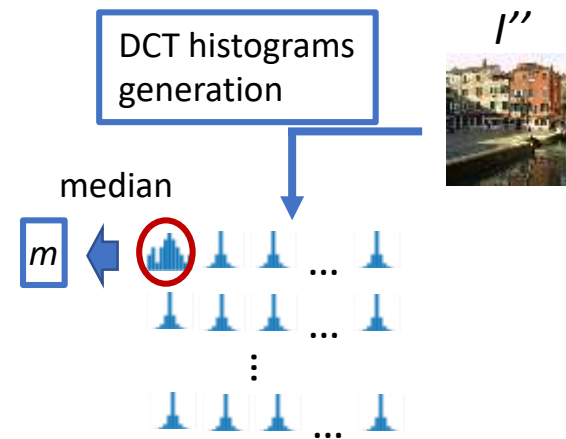
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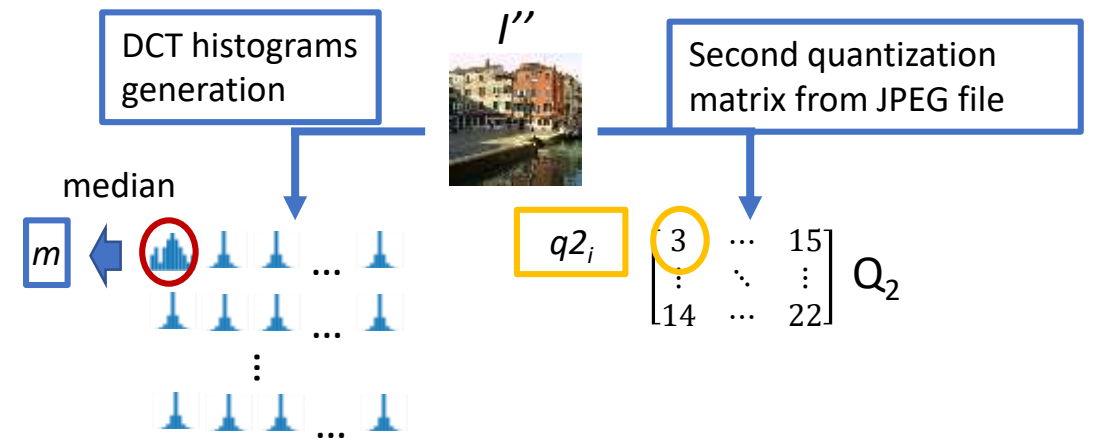
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Q_1

First quantization matrix Q_1

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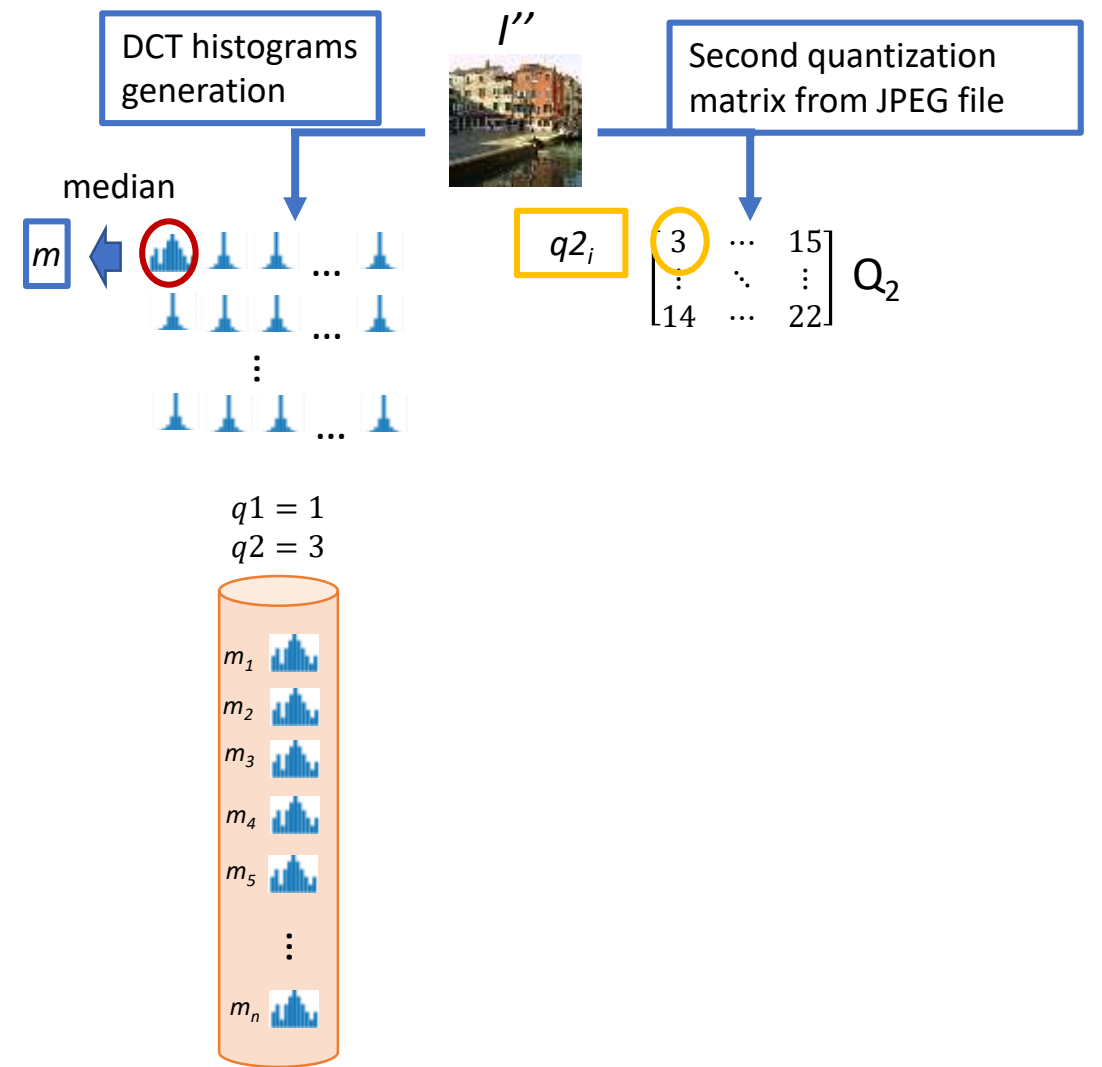
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18: regularize( $\{q1_1, q1_2, \dots, q1_k\}$ )
19: return  $\{q1_1, q1_2, \dots, q1_k\}$ 

```



$\begin{bmatrix} \dots \\ \vdots \\ \dots \end{bmatrix}$

First quantization matrix Q_1

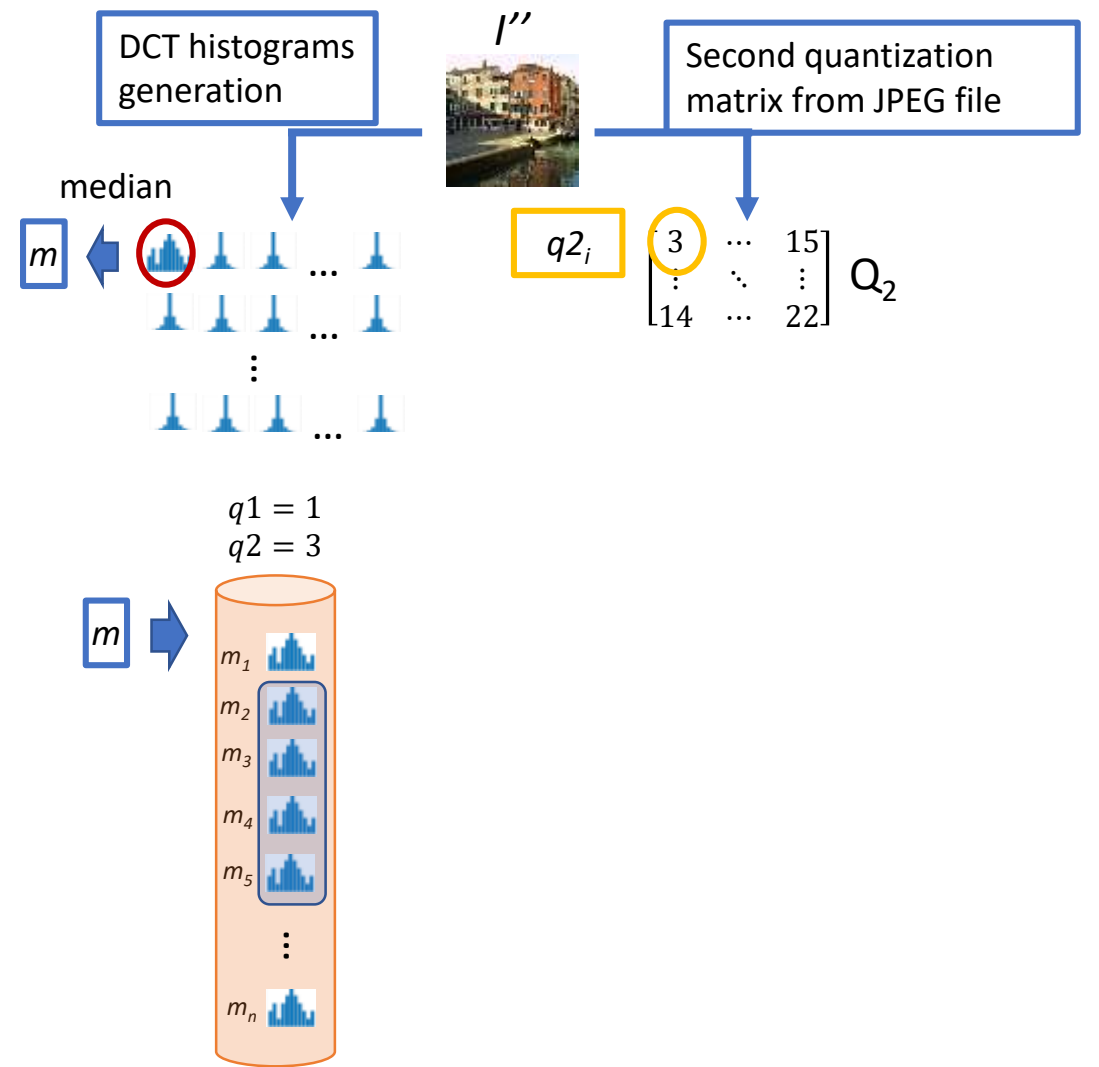
Algorithm 1 The Proposed FQE Technique

Input: double compressed image I''

Output: $\{q1_1, q1_2, \dots, q1_k\}$

Initialization : $k, q1_{max}$

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1: for  $i = 1$  to  $k$  do
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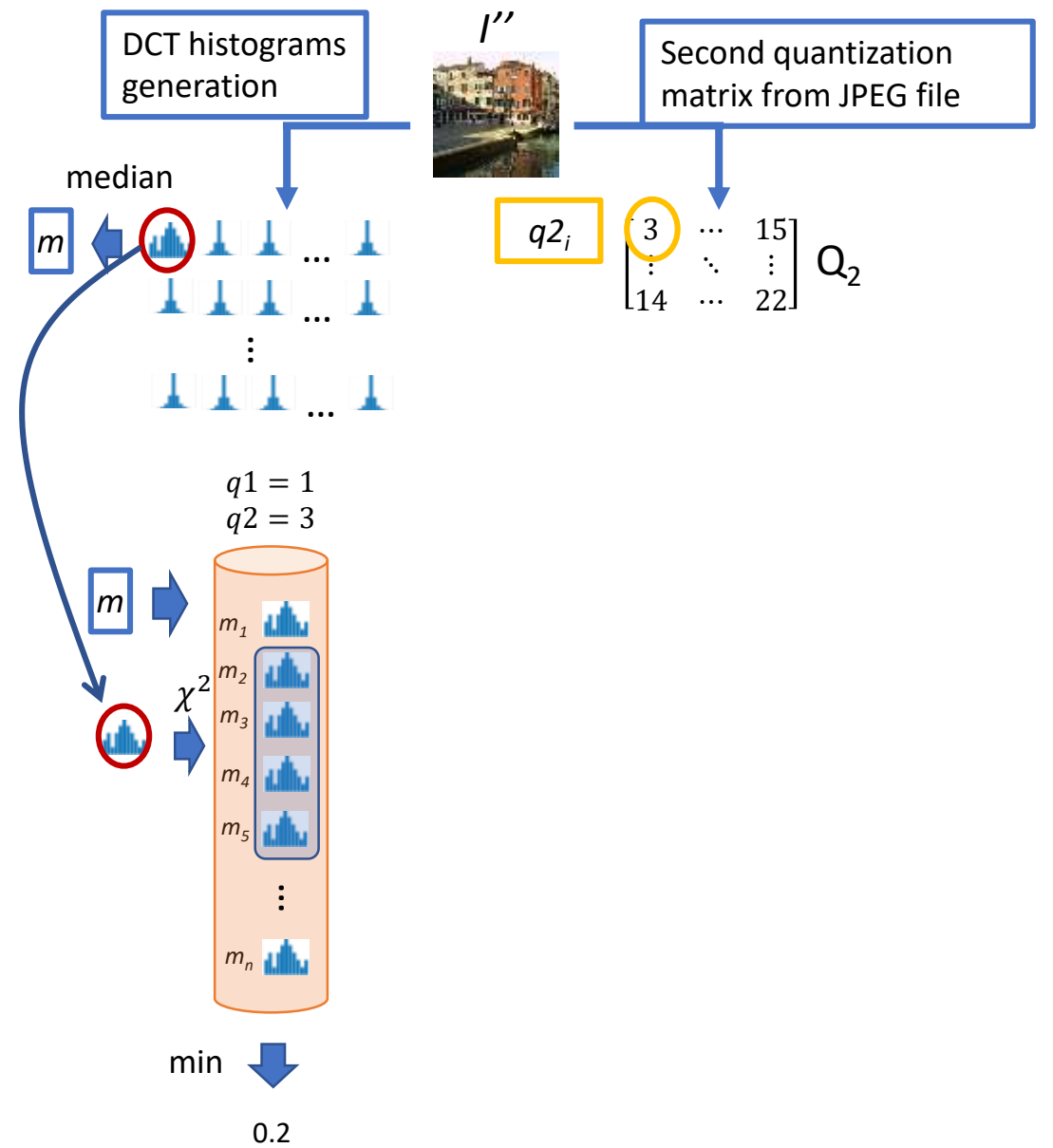
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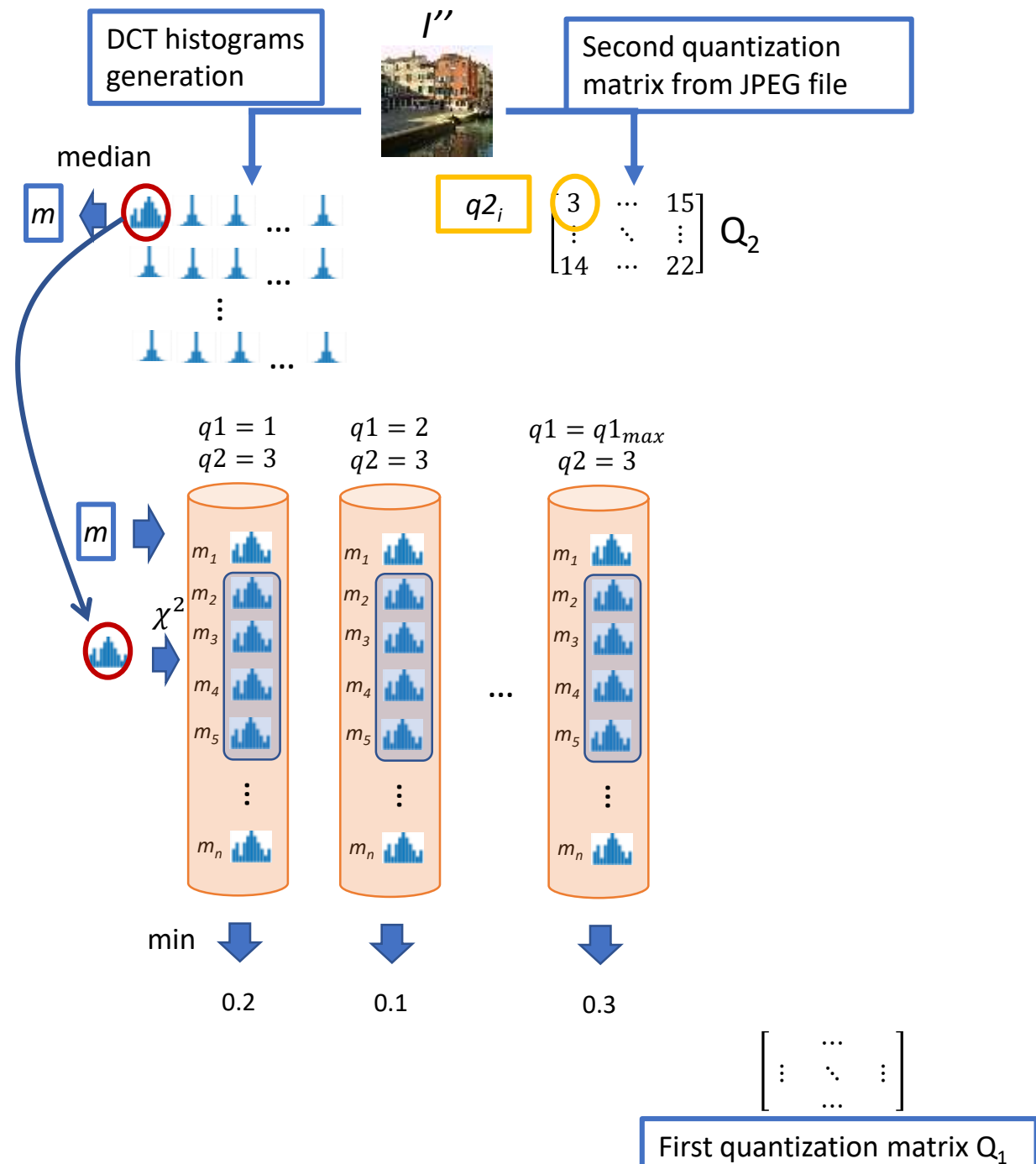
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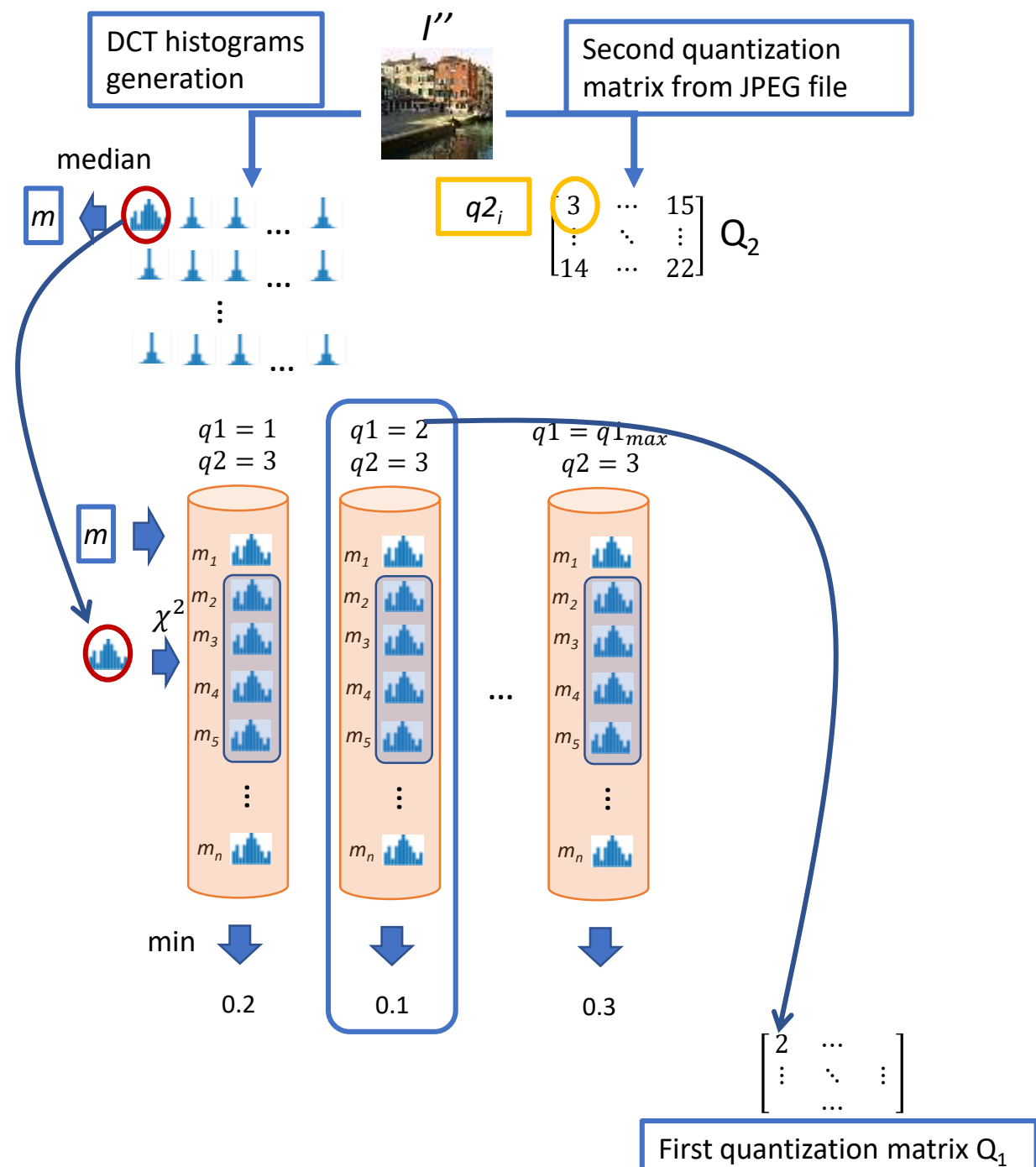
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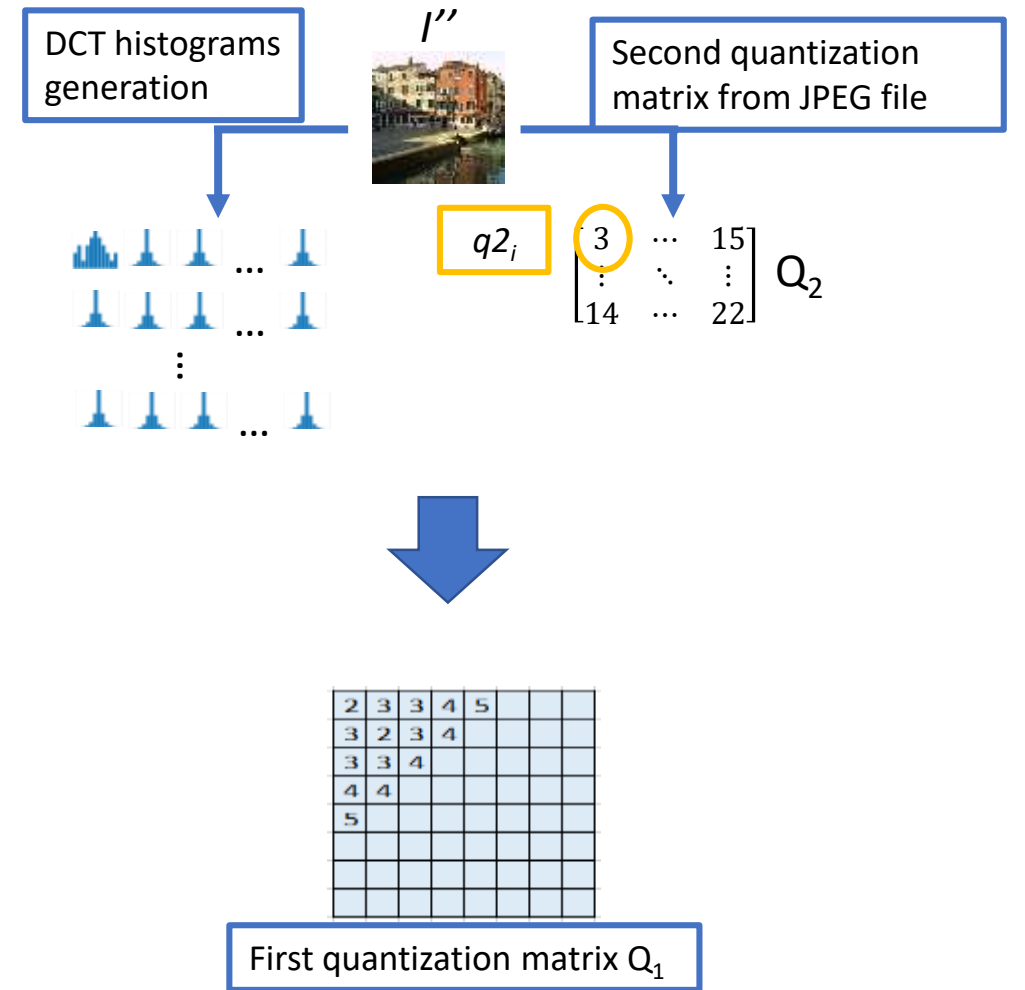
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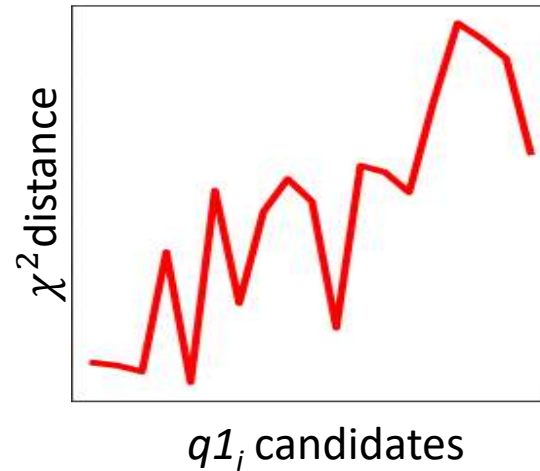


Regularization

- Sometimes, the information contained in h_i does not clearly allow the discrimination among the possible $q1_i$ candidates.

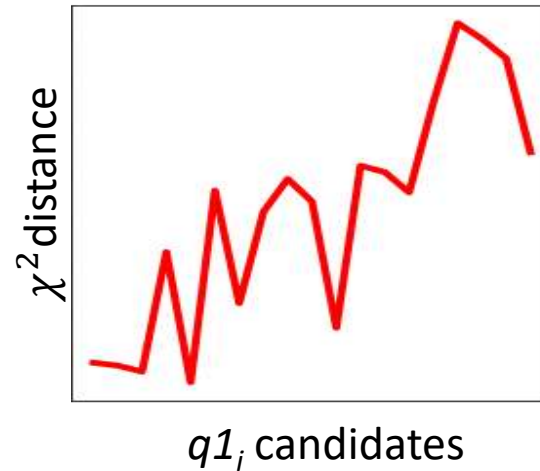
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- A strong minimum is not always present at varying of $q1_i$ candidates.

Regularization

- Data coming from neighbors DCT coefficients can be exploited.

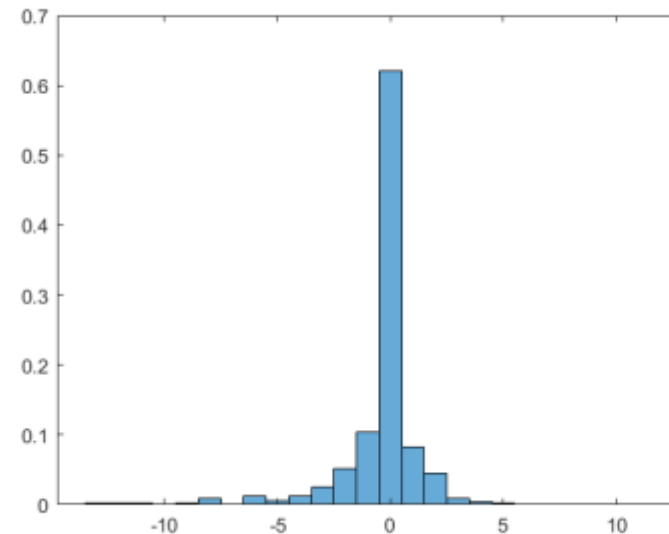
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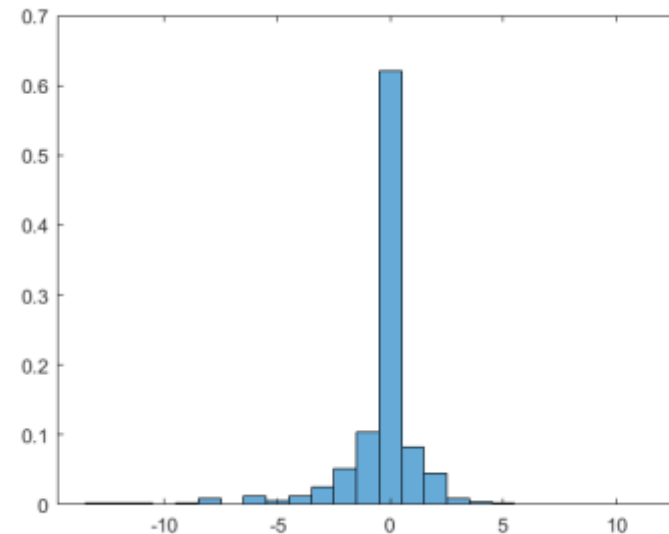
Distribution of $q1_i - q1_{i+1}$ built considering custom tables from Park et al. and $q1_{max} < 22$.



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- Instead of estimating each coefficient independently, three consecutive elements in zig-zag order are considered.

Distribution of $q1_i - q1_{i+1}$ built considering custom tables from Park et al. and $q1_{max} < 22$.



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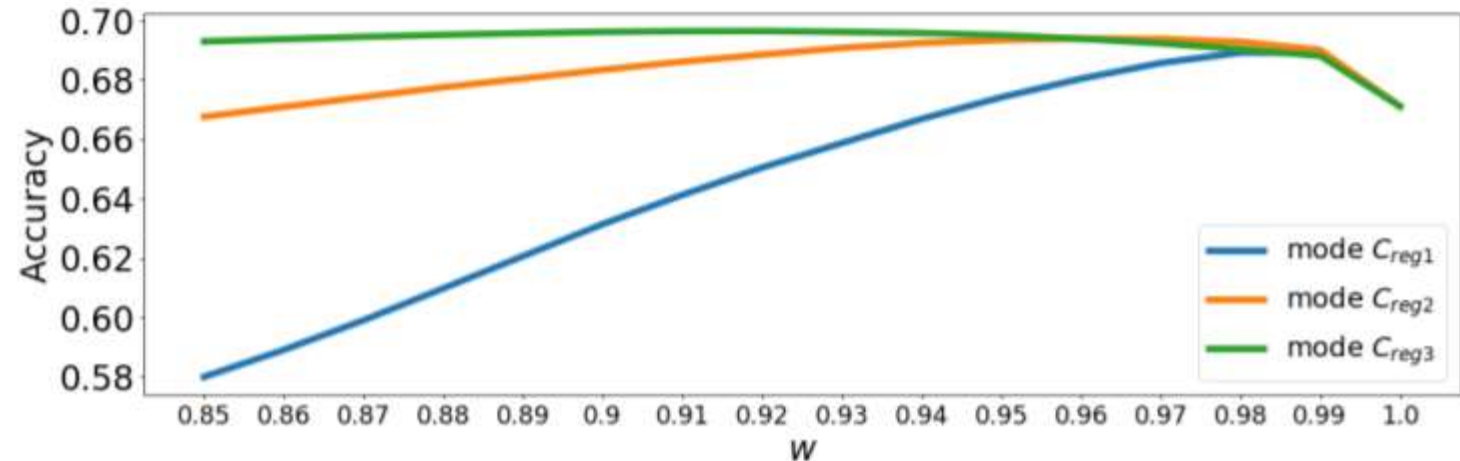
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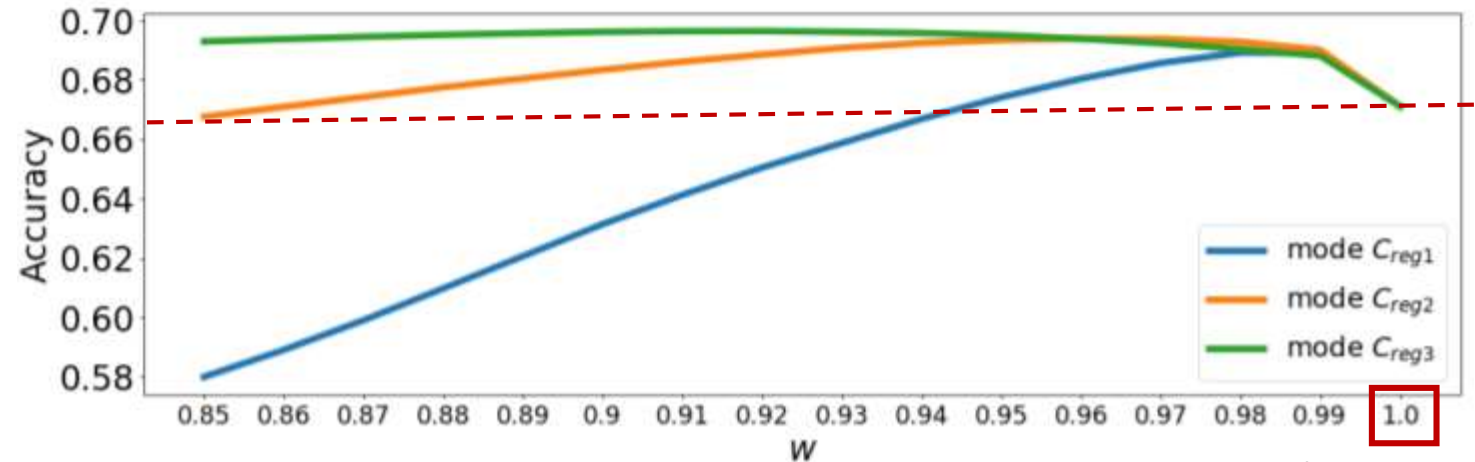
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without regularization

Regularization

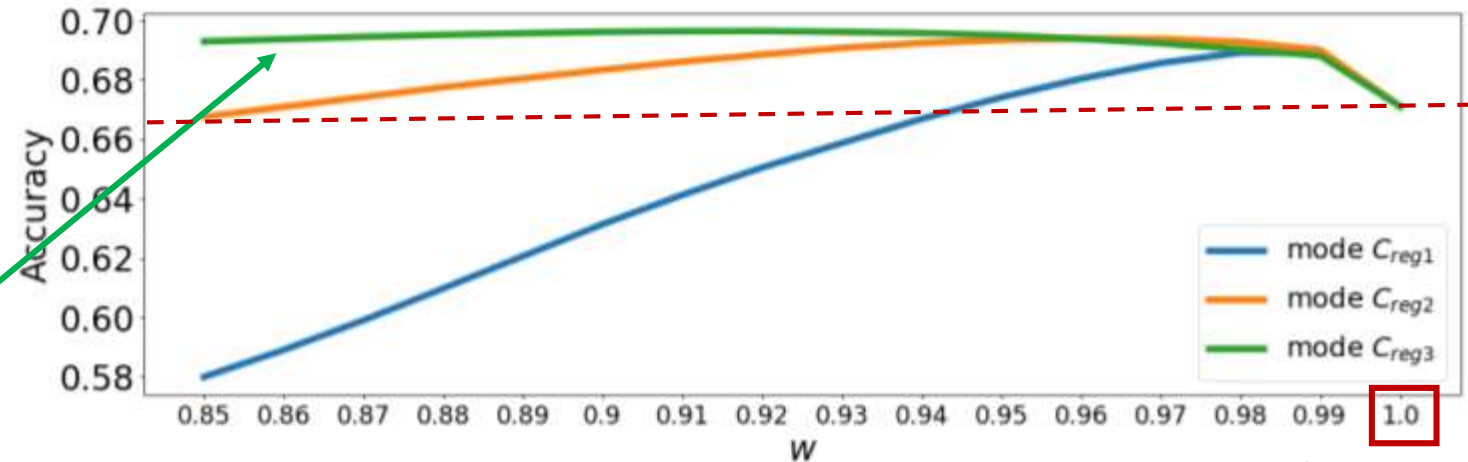
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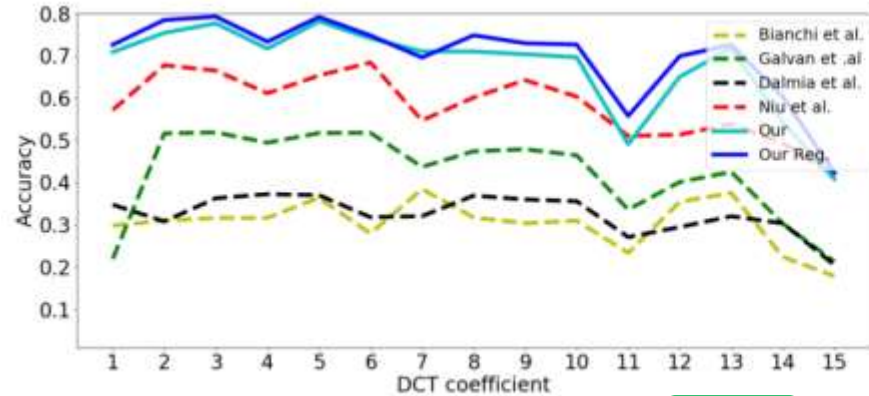
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without regularization

Experimental results (comparisons)

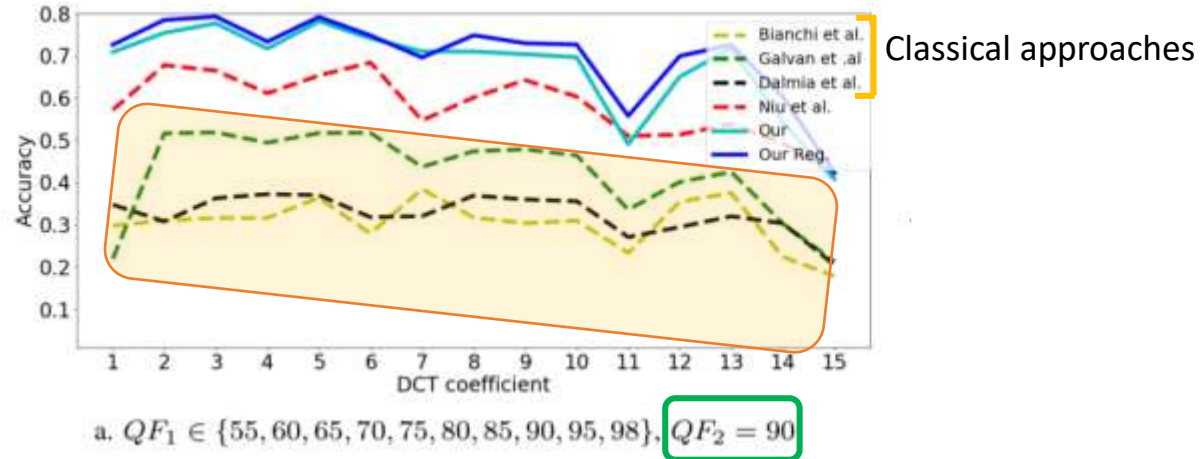
Standard
Matrices



a. $QF_1 \in \{55, 60, 65, 70, 75, 80, 85, 90, 95, 98\}$, $QF_2 = 90$

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T. Bianchi and A. Piva, "Image forgery localization via block-grained analysis of JPEG artifacts," Proc. of IEEE Trans. on Information Forensics and Security, vol. 7, no. 3, p. 1003, 2012.

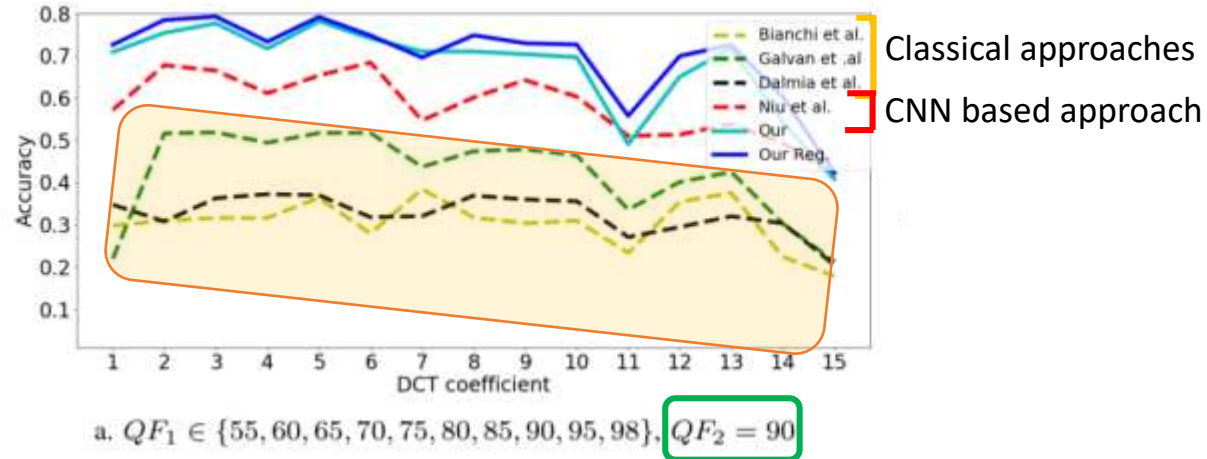
F. Galvan, G. Puglisi, A. R. Bruna, and S. Battiato, "First quantization matrix estimation from double compressed JPEG images," IEEE Trans. on Information Forensics and Security, vol. 9, no. 8, pp. 1299–1310, 2014.

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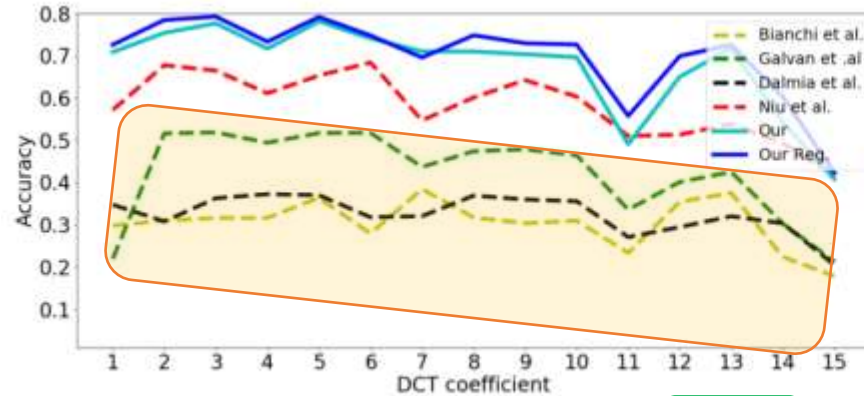
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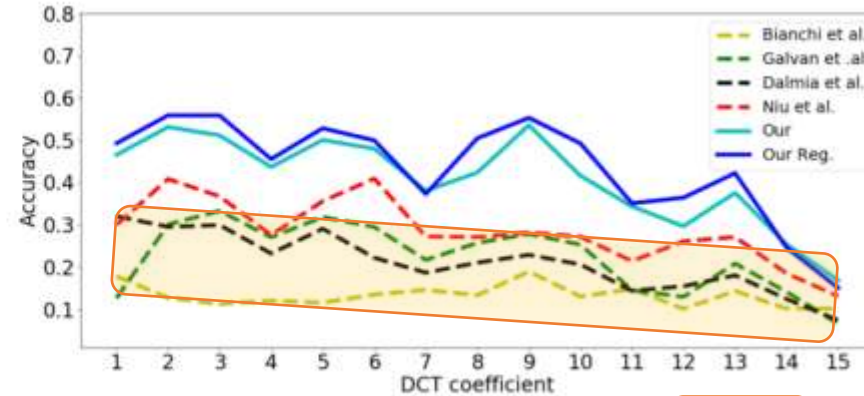


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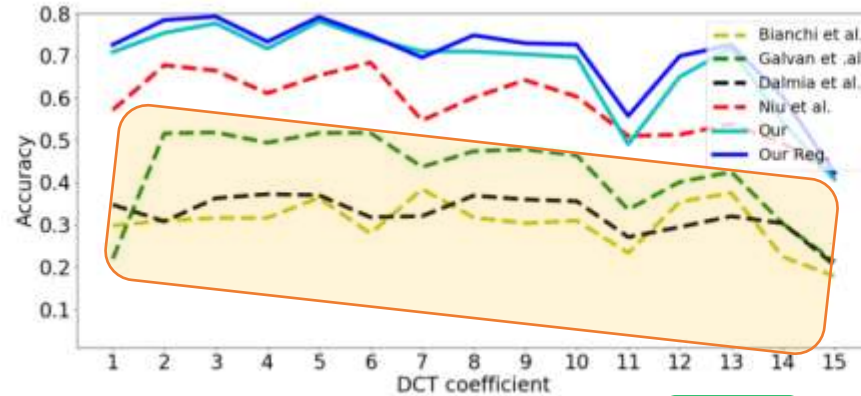
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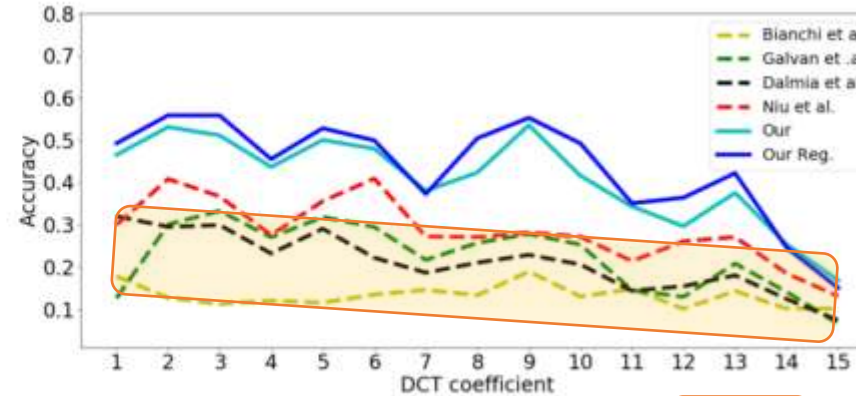
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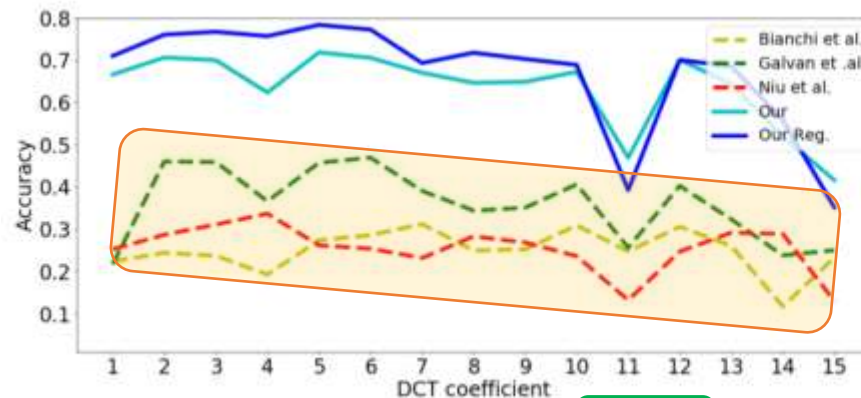


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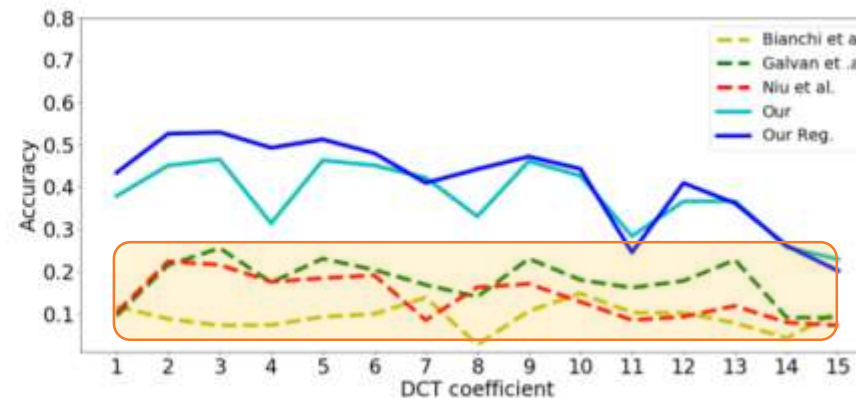


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Photoshop
Custom
Matrices



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Method	Dataset	Cropped Patch	Low/Low	Low/Mid	Low/High	Mid/Low	Mid/Mid	Mid/High	High/Low	High/Mid	High/High	Mean
Our	RAISE	64 × 64	0.25	0.47	0.79	0.17	0.32	0.82	0.27	0.31	0.70	0.46
Our Reg.			0.30	0.53	0.81	0.22	0.37	0.84	0.25	0.33	0.75	0.49
Our	UCID	64 × 64	0.33	0.63	0.93	0.20	0.39	0.90	0.15	0.21	0.66	0.49
Our Reg.			0.36	0.65	0.96	0.23	0.42	0.91	0.13	0.23	0.73	0.51
Our	RAISE	128 × 128	0.36	0.60	0.85	0.29	0.44	0.87	0.25	0.32	0.74	0.52
Our Reg.			0.41	0.55	0.88	0.34	0.48	0.89	0.25	0.38	0.79	0.55
Our	UCID	128 × 128	0.47	0.76	0.96	0.31	0.49	0.94	0.18	0.29	0.74	0.57
Our Reg.			0.50	0.79	0.96	0.35	0.51	0.93	0.20	0.34	0.79	0.60
Our	RAISE	256 × 256	0.45	0.69	0.88	0.38	0.52	0.89	0.25	0.36	0.77	0.58
Our Reg.			0.49	0.73	0.90	0.40	0.55	0.90	0.30	0.45	0.82	0.62
Our	UCID	256 × 256	0.56	0.83	0.98	0.44	0.57	0.96	0.23	0.34	0.77	0.63
Our Reg.			0.60	0.85	0.97	0.48	0.60	0.96	0.28	0.43	0.82	0.67
Our	RAISE	512 × 512	0.50	0.74	0.91	0.44	0.57	0.91	0.26	0.38	0.77	0.61
Our Reg.			0.50	0.78	0.92	0.48	0.59	0.92	0.32	0.48	0.83	0.65
Our	UCID	Full size	0.63	0.86	0.98	0.51	0.62	0.96	0.27	0.39	0.80	0.66
Our Reg.			0.67	0.87	0.97	0.56	0.62	0.96	0.37	0.49	0.85	0.71

J. Park, D. Cho, W. Ahn, and H. Lee, "Double JPEG detection in mixed JPEG quality factors using deep convolutional neural network," in The European Conference on Computer Vision (ECCV), September 2018.

D. Dang-Nguyen, C. Pasquini, V. Conotter, and G. Boato, "Raise: a raw images dataset for digital image forensics," in Proc. of the 6th ACM Multimedia Systems Conference, 2015, pp. 219–224.

G. Schaefer and M. Stich, "UCID: An uncompressed color image database," in Storage and Retrieval Methods and Applications for Multimedia 2004, vol. 5307. International Society for Optics and Photonics, 2003, pp. 472–480.

Experimental results (custom tables)

Park et al. collected a dataset of JPEG quantization matrices employed in real scenarios.

To evaluate the generalization capability of the proposed solution a series of tests have been conducted considering these quantization matrices divided into three groups: Low, Mid, High.

[0,0.33[

[0.33,0.66[

[0.66,1]

Method	Dataset	Cropped Patch	Low/Low	Low/Mid	Low/High	Mid/Low	Mid/Mid	Mid/High	High/Low	High/Mid	High/High	Mean
Our	RAISE	64 × 64	0.25	0.47	0.79	0.17	0.32	0.82	0.27	0.31	0.70	0.46
Our Reg.			0.30	0.53	0.81	0.22	0.37	0.84	0.25	0.33	0.75	0.49
Our	UCID	64 × 64	0.33	0.63	0.93	0.20	0.39	0.90	0.15	0.21	0.66	0.49
Our Reg.			0.36	0.65	0.96	0.23	0.42	0.91	0.13	0.23	0.73	0.51
Our	RAISE	128 × 128	0.36	0.60	0.85	0.29	0.44	0.87	0.25	0.32	0.74	0.52
Our Reg.			0.41	0.55	0.88	0.34	0.48	0.89	0.25	0.38	0.79	0.55
Our	UCID	128 × 128	0.47	0.76	0.96	0.31	0.49	0.94	0.18	0.29	0.74	0.57
Our Reg.			0.50	0.79	0.96	0.35	0.51	0.93	0.20	0.34	0.79	0.60
Our	RAISE	256 × 256	0.45	0.69	0.88	0.38	0.52	0.89	0.25	0.36	0.77	0.58
Our Reg.			0.49	0.73	0.90	0.40	0.55	0.90	0.30	0.45	0.82	0.62
Our	UCID	256 × 256	0.56	0.83	0.98	0.44	0.57	0.96	0.23	0.34	0.77	0.63
Our Reg.			0.60	0.85	0.97	0.48	0.60	0.96	0.28	0.43	0.82	0.67
Our	RAISE	512 × 512	0.50	0.74	0.91	0.44	0.57	0.91	0.26	0.38	0.77	0.61
Our Reg.			0.50	0.78	0.92	0.48	0.59	0.92	0.32	0.48	0.83	0.65
Our	UCID	Full size	0.63	0.86	0.98	0.51	0.62	0.96	0.27	0.39	0.80	0.66
Our Reg.			0.67	0.87	0.97	0.56	0.62	0.96	0.37	0.49	0.85	0.71

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Conclusions

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- Finally, the use of 1-nn to learn the distribution underlines rooms for improvement of the proposed method.

Thank you!

In-Depth DCT Coefficient Distribution Analysis for First Quantization Estimation

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